



Attempt the following questions.

№ of Questions: 3 in 2 page(s)
Total Mark: 30

Question 1: (10 Marks)

Consider the problem of adding two n -bit binary integers, stored in two n -element arrays A and B . The sum of the two integers should be stored in binary form in an $(n+1)$ -element array C . State the problem formally and write pseudocode for adding the two integers.

Question 2: (10 Marks)

Use a recursion tree to give an asymptotically tight solution to the recurrence $T(n) = T(\alpha n) + T((1 - \alpha)n) + cn$, where α is a constant in the range $0 < \alpha < 1$ and $c > 0$ is also a constant. Verify your solution by the substitution method.

Question 3: (10 Marks)

Suppose that instead of swapping element $A[i]$ with a random element from the subarray $A[i..n]$, we swapped it with a random element from anywhere in the array:

```
PERMUTE-WITH-ALL (A)
1   $n = A.length$ 
2  for  $i = 1$  to  $n$ 
3      swap  $A[i]$  with  $A[RANDOM(1, n)]$ 
```

Does this code produce a uniform random permutation? Why or why not?

Good Luck
Dr. Islam ElShaarawy

